

Задание 1

Передаточная функция линейной САУ

Вывести формулу передаточной функции по заданному дифференциальному уравнению. Написать формулу характеристического уравнения.

Пример решения см. в учебном пособии (есть в библиотеке ЛГТУ):

Музылёва И. В. Теория автоматического управления. Линейные системы [Текст]: методические указания к практическим занятиям / И. В. Музылева, А. А. Муравьев. - Липецк: Изд-во ЛГТУ, 2013. - 79 с.

Варианты задания

| № | Дифференциальное уравнение |
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| 1 | $-33\frac{d^3x_{\text{вых}}(t)}{dt^3} + 22\frac{d^2x_{\text{вых}}(t)}{dt^2} + 11\frac{dx_{\text{вых}}(t)}{dt} = 22\frac{dx_{\text{вх}}(t)}{dt} + 11x_{\text{вх}}(t)$ |
| 2 | $3\frac{d^4x_{\text{вых}}(t)}{dt^4} + 9\frac{d^3x_{\text{вых}}(t)}{dt^3} + 3\frac{d^2x_{\text{вых}}(t)}{dt^2} = 6\frac{d^2x_{\text{вх}}(t)}{dt^2} - 9x_{\text{вх}}(t)$ |
| 3 | $3\frac{d^4x_{\text{вых}}(t)}{dt^4} + 2\frac{d^3x_{\text{вых}}(t)}{dt^3} - \frac{dx_{\text{вых}}(t)}{dt} + 10x_{\text{вых}}(t) = \frac{dx_{\text{вх}}(t)}{dt}x_{\text{вх}}(t) + 10x_{\text{вх}}(t)$ |
| 4 | $\frac{d^4x_{\text{вых}}(t)}{dt^4} + 6\frac{d^2x_{\text{вых}}(t)}{dt^2} + \frac{dx_{\text{вых}}(t)}{dt} + 30x_{\text{вых}}(t) = 9\frac{d^3x_{\text{вх}}(t)}{dt^3} - 6\frac{d}{dt}x_{\text{вх}}(t)$ |
| 5 | $14\frac{d^5x_{\text{вых}}(t)}{dt^5} + 7\frac{d^2x_{\text{вых}}(t)}{dt^2} - 14\frac{dx_{\text{вых}}(t)}{dt} + x_{\text{вых}}(t) = 7\frac{d^2x_{\text{вх}}(t)}{dt^2} + \frac{dx_{\text{вх}}(t)}{dt}$ |
| 6 | $8\frac{d^3x_{\text{вых}}(t)}{dt^3} + \frac{d^2x_{\text{вых}}(t)}{dt^2} - 12\frac{dx_{\text{вых}}(t)}{dt} + 4x_{\text{вых}}(t) = -4\frac{d^3x_{\text{вх}}(t)}{dt^3} + 0,4x_{\text{вх}}(t)$ |
| 7 | $1,5\frac{d^6x_{\text{вых}}(t)}{dt^6} - 9\frac{d^3x_{\text{вых}}(t)}{dt^3} + 1,2\frac{dx_{\text{вых}}(t)}{dt} + 3x_{\text{вых}}(t) = 0,6\frac{d^2x_{\text{вх}}(t)}{dt^2}$ |
| 8 | $4\frac{d^4x_{\text{вых}}(t)}{dt^4} + 0,8\frac{d^2x_{\text{вых}}(t)}{dt^2} - \frac{dx_{\text{вых}}(t)}{dt} = 6\frac{d^2x_{\text{вх}}(t)}{dt^2} + 0,2\frac{dx_{\text{вх}}(t)}{dt}$ |
| 9 | $66\frac{d^5x_{\text{вых}}(t)}{dt^5} - 33\frac{d^3x_{\text{вых}}(t)}{dt^3} + 11\frac{dx_{\text{вых}}(t)}{dt} + 22x_{\text{вых}}(t) = 11x_{\text{вх}}(t)$ |
| 10 | $12\frac{d^5x_{\text{вых}}(t)}{dt^5} + 6\frac{d^2x_{\text{вых}}(t)}{dt^2} - 12\frac{dx_{\text{вых}}(t)}{dt} + 1,2x_{\text{вых}}(t) = 2\frac{d^4x_{\text{вх}}(t)}{dt^4} + 4x_{\text{вх}}(t)$ |

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| 11 | $2\frac{d^3x_{\text{бблх}}(t)}{dt^3} - 7\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 9\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 8\frac{d^2x_{\text{бх}}(t)}{dt^2} x_{\text{бх}}(t) + x_{\text{бх}}(t)$ |
| 12 | $3\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 1,5\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 5\frac{d^2x_{\text{бблх}}(t)}{dt^2} - \frac{dx_{\text{бблх}}(t)}{dt} + 10x_{\text{бблх}}(t) = 2x_{\text{бх}}(t)$ |
| 13 | $30\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 3\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 9\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 3\frac{dx_{\text{бх}}(t)}{dt}$ |
| 14 | $1,2\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 3,6\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 9\frac{d^2x_{\text{бх}}(t)}{dt^2} - 3x_{\text{бх}}(t)$ |
| 15 | $-3,3\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 2,2\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 1,1\frac{dx_{\text{бблх}}(t)}{dt} = 2,2\frac{dx_{\text{бх}}(t)}{dt} + 11x_{\text{бх}}(t)$ |
| 16 | $3\frac{d^6x_{\text{бблх}}(t)}{dt^6} + 0,9\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 0,3\frac{d^2x_{\text{бблх}}(t)}{dt^2} = 0,6\frac{d^2x_{\text{бх}}(t)}{dt^2} - 0,3x_{\text{бх}}(t)$ |
| 17 | $50\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 25\frac{d^3x_{\text{бблх}}(t)}{dt^3} - \frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 5\frac{dx_{\text{бх}}(t)}{dt} x_{\text{бх}}(t) + x_{\text{бх}}(t)$ |
| 18 | $\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 1,2\frac{dx_{\text{бблх}}(t)}{dt} + 3x_{\text{бблх}}(t) = 9\frac{d^3x_{\text{бх}}(t)}{dt^3} - 6x_{\text{бх}}(t)$ |
| 19 | $4\frac{d^5x_{\text{бблх}}(t)}{dt^5} + \frac{d^2x_{\text{бблх}}(t)}{dt^2} - 14\frac{d}{dt}x_{\text{бблх}}(t) + x_{\text{бблх}}(t) = 7\frac{d^2x_{\text{бх}}(t)}{dt^2} + 21\frac{dx_{\text{бх}}(t)}{dt}$ |
| 20 | $3\frac{d^4x_{\text{бблх}}(t)}{dt^4} - 1,5\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 2,5\frac{d^2x_{\text{бблх}}(t)}{dt^2} - \frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 2x_{\text{бх}}(t)$ |
| 21 | $30\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 3\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 9\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 3\frac{dx_{\text{бх}}(t)}{dt}$ |
| 22 | $18\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 3,6\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 5\frac{d^2x_{\text{бх}}(t)}{dt^2} - 3,6x_{\text{бх}}(t)$ |
| 23 | $-3,3\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 2,2\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 1,1\frac{dx_{\text{бблх}}(t)}{dt} = 2,2\frac{dx_{\text{бх}}(t)}{dt}$ |
| 24 | $30\frac{d^6x_{\text{бблх}}(t)}{dt^6} - 0,9\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 0,3\frac{d^2x_{\text{бблх}}(t)}{dt^2} = 6\frac{d^2x_{\text{бх}}(t)}{dt^2} - 0,3x_{\text{бх}}(t)$ |
| 25 | $5\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 25\frac{d^2x_{\text{бблх}}(t)}{dt^2} - \frac{dx_{\text{бблх}}(t)}{dt} + 5x_{\text{бблх}}(t) = 5\frac{dx_{\text{бх}}(t)}{dt} x_{\text{бх}}(t) + x_{\text{бх}}(t)$ |
| 26 | $\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 1,2\frac{dx_{\text{бблх}}(t)}{dt} + 3x_{\text{бблх}}(t) = 9\frac{d^2x_{\text{бх}}(t)}{dt^2} - 6x_{\text{бх}}(t)$ |
| 27 | $3\frac{d^6x_{\text{бблх}}(t)}{dt^6} - 0,9\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 0,3\frac{d^2x_{\text{бблх}}(t)}{dt^2} = 0,6\frac{d^2x_{\text{бх}}(t)}{dt^2} - 0,3x_{\text{бх}}(t)$ |
| 28 | $50\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 25\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 5\frac{dx_{\text{бблх}}(t)}{dt} + 10x_{\text{бблх}}(t) = 5\frac{dx_{\text{бх}}(t)}{dt} + x_{\text{бх}}(t)$ |
| 29 | $5\frac{d^5x_{\text{бблх}}(t)}{dt^5} - 33\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 1,1\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 44\frac{d^3x_{\text{бх}}(t)}{dt^3} + 11x_{\text{бх}}(t)$ |

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| 30 | $12\frac{d^5x_{\text{бблх}}(t)}{dt^3} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 12\frac{dx_{\text{бблх}}(t)}{dt} + 1,2x_{\text{бблх}}(t) = \frac{d^4x_{\text{гх}}(t)}{dt^4} + x_{\text{гх}}(t)$ |
| 31 | $2\frac{d^3x_{\text{бблх}}(t)}{dt^3} - \frac{d^2x_{\text{бблх}}(t)}{dt^2} - 9\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = -\frac{d^2x_{\text{гх}}(t)}{dt^2}x_{\text{гх}}(t) + 4x_{\text{гх}}(t)$ |
| 32 | $30\frac{d^5x_{\text{бблх}}(t)}{dt^5} + 1,5\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 25\frac{d^2x_{\text{бблх}}(t)}{dt^2} - \frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 2x_{\text{гх}}(t)$ |
| 33 | $30\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 3\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 9\frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 3\frac{dx_{\text{гх}}(t)}{dt}$ |
| 34 | $9\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 36\frac{dx_{\text{бблх}}(t)}{dt} + 0,9x_{\text{бблх}}(t) = 9\frac{d^2x_{\text{гх}}(t)}{dt^2} - 3x_{\text{гх}}(t)$ |
| 35 | $-33\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 22\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 11\frac{dx_{\text{бблх}}(t)}{dt} = 77\frac{dx_{\text{гх}}(t)}{dt} + 11x_{\text{гх}}(t)$ |
| 36 | $0,3\frac{d^6x_{\text{бблх}}(t)}{dt^6} + 9\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 0,3\frac{d^2x_{\text{бблх}}(t)}{dt^2} = 6\frac{d^2x_{\text{гх}}(t)}{dt^2} - 0,3x_{\text{гх}}(t)$ |
| 37 | $5\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 250\frac{d^3x_{\text{бблх}}(t)}{dt^3} - \frac{dx_{\text{бблх}}(t)}{dt} + x_{\text{бблх}}(t) = 5\frac{dx_{\text{гх}}(t)}{dt}x_{\text{гх}}(t) + x_{\text{гх}}(t)$ |
| 38 | $12\frac{d^4x_{\text{бблх}}(t)}{dt^4} + 6\frac{d^2x_{\text{бблх}}(t)}{dt^2} + 12\frac{dx_{\text{бблх}}(t)}{dt} + 3x_{\text{бблх}}(t) = 24\frac{d^3x_{\text{гх}}(t)}{dt^3} - 6x_{\text{гх}}(t)$ |
| 39 | $1,4\frac{d^5x_{\text{бблх}}(t)}{dt^5} + 7\frac{d^2x_{\text{бблх}}(t)}{dt^2} - 14\frac{d}{dt}x_{\text{бблх}}(t) + 7x_{\text{бблх}}(t) = -2,1\frac{dx_{\text{гх}}(t)}{dt}$ |
| 40 | $3\frac{d^4x_{\text{бблх}}(t)}{dt^4} - 1,5\frac{d^3x_{\text{бблх}}(t)}{dt^3} + 5\frac{d^2x_{\text{бблх}}(t)}{dt^2} - \frac{dx_{\text{бблх}}(t)}{dt} + 100x_{\text{бблх}}(t) = 2x_{\text{гх}}(t)$ |